

Exercise N° 1 :

$$1) V = \frac{4}{3} \pi r^3 \rightarrow \rho_g = \frac{m_T}{V_T} = \frac{10^6}{\frac{4}{3} \pi r^3} \rightarrow r = \sqrt[3]{\frac{10^6}{\frac{4}{3} \pi r^3}} = 6,215 \text{ m}$$

$$F = \frac{V_{immer}}{V_{total}} \cdot 100 = \frac{\rho_{glace}}{\rho_e} \cdot 100 = \frac{995}{1025} \cdot 100 = 97 \%$$

$$2) F_{arch} = P_G \Rightarrow \rho_{ice} \cdot g \cdot V_{total} = \rho_e \cdot g \cdot V_{immer}$$

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$$3) \frac{V_{immer}}{V_{total}} = \frac{\rho_{ice}}{\rho_e} \Rightarrow V_{immer} = V_{total} \cdot \frac{\rho_{ice}}{\rho_e} = 975,61 \text{ m}^3$$

4) The volume fraction F is independent of the shape of the body, it has the relation only with the ratio of the densities, therefore F=97%.

Exercise N° 2 :

$$1) P_{weight} = P_{ARCH} = F_1 \cdot V \cdot \rho_{mer} \cdot g = F_1 \cdot \frac{4}{3} \pi \cdot R^3 \cdot \rho_{mer} \cdot g \quad P_{weight} = \frac{1}{2} \frac{4}{3} \pi \cdot 0,1^3 \cdot 1025 \cdot 9,81 = 21 \text{ N}$$

$$2) P_{weight} = P_{ARCH} \Leftrightarrow F_2 \cdot V \cdot \rho_{oil} \cdot g = P_{weight} \quad F_2 = \frac{1}{2} \frac{\rho_{mer}}{\rho_{oil}} \quad \text{A.N.} \quad F_2 = \frac{1}{2} \frac{1025}{800} = 64 \%$$

Exercise N° 3 :

1) If we neglect the atmospheric pressure, the resultant of the pressure forces:

$$= P_G \cdot S \cdot \vec{X} \quad \text{with: } S = a \cdot b \quad \text{So: } \|\vec{R}\| = \rho \cdot g \cdot S \cdot Z_g \quad \text{A.N.} \quad \|\vec{R}\| = 1000 \cdot 9,81 \cdot 6,4 = 235440 \text{ N}$$

2) The depth Z_R of the center of pressure is given by the following expression:

$$Z_R = \frac{I_{(G,Y)}}{Z_G \cdot S} + Z_G \quad \text{Or: } I_{(G,Y)} = \frac{2^3 \cdot 3}{12} = 2 \text{ m}^4 \quad \text{A.N.} \quad Z_R = 4,0833 \text{ m}$$

3) Case of a glazed part of circular shape with a diameter d= 2 m:

$$S = \frac{\pi \cdot d^2}{4} = 3,141 \text{ m}^2, \quad I_{(G,Y)} = \frac{\pi \cdot d^4}{64} = 0,785 \text{ m}^4$$

$$\|\vec{R}\| = \rho \cdot g \cdot S \cdot Z_g \quad \text{A.N.} \quad \|\vec{R}\| = 123252 \text{ N} \quad Z_R = \frac{I_{(G,Y)}}{Z_G \cdot S} + Z_G \quad \text{A.N.} \quad Z_R = \frac{0,785}{4,314} + 4 = 4,0625 \text{ m}$$